

Orbit Correction Within Constrained Solution Spaces



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Constraints for Orbit Correction

- i. Hardware limitation of physical corrector strengths
 - Global orbit correction on a misaligend (low emittance) magnet lattice
 - Local orbit bumps of increased amplitude (aperture scans, BBC, etc)
 - Enhanced by:
 - Little maximum corrector strengths
 - Little Phase advances (low tune)
 - Calibrational errors of BPM offsets
- ii. Solution space of local impact (bumps)

iii. Exploitation of nullspace



DELTA Corrector Design







Corrector Coils Magnetic Field Electron Beam Resulting Deflection



Corrector Strength

- <u>horizontal correctors</u>:
 - long γoke (40cm):
 2×150 windings
 max: 3.0-1.8 mrad @ 1.5 GeV
 - short yoke (20cm):
 2x240 windings
 max: 3.0-1.5 mrad @ 1.5 GeV
- vertical correctors:
 - short yokes only:
 4x50 windings
 max: 1.1 0.5 mrad @ 1.5 GeV





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University of Dortmund Significance of Calibration Errors bpm16 - 100µm Correction of simulated offsets for: bpm17 +100µm 0.2 1.00.1 **Displacement** [mm] 0.0 Kick [mrad] -0.1 vertical 0.5 bpm16: +100µm -0.2 bpm17: -100µm -0.3 0.0-0.4 -0.5 pm42 pm46 pm47 pm47 pm49 pm50 pm51 pm52 pm52 pm52 pm14 pm15pm31 pm32 pm35 pm35 pm35 pm36 pm38 pm39 pm40 pm41 pm44k03 k08 k10 k12 k12 k12 • Large corrector strengths afforded (>0.5 out of 0.5 to 1.1 mrad max) • Error propagatation (1.2mm !!)

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SVD-Based Orbit Correction

$$\begin{pmatrix} w_1 & 0 \\ & \ddots & \\ 0 & & w_m \end{pmatrix} \begin{pmatrix} \vec{R}_1 \vec{R}_2 \vec{R}_3 \cdots \vec{R}_n \\ \end{bmatrix} \Rightarrow \mathbf{W} \mathbf{R} \Rightarrow \mathbf{U} [\operatorname{diag}(\boldsymbol{\sigma}_i)] \mathbf{V}^{\mathrm{T}} \\ \mathbf{U}^{\mathrm{T}} \mathbf{U} = \mathbf{V}^{\mathrm{T}} \mathbf{V} = \mathbf{V} \mathbf{V}^{\mathrm{T}} = \mathbf{1}$$

Inverse within the
Range of WR
(Pseudoinverse): $(WR)^{\#} = V[\operatorname{diag}(1/\sigma_i)]U^{T}$
 $\vec{\theta}_{OC} = -\mathbf{R}^{\#} \Delta \vec{K}$
 $\|W(\mathbf{R}\vec{\theta}_{OC} + \Delta \vec{K})\|_{2} \rightarrow \min.$



Free Parameter for SVD-Based matrix inversion:





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Solutions for Constraining Correctors ?

Relative corrector strength



- rather ficticious task here
- typical for DELTA about 2 limited correctors vertically (usually no problems horizontally)





 \rightarrow Find the closest spot to a given point on a set of hyperplanes in **n** dimensions

 $\left\| \mathbf{U}^{\mathrm{T}} \mathbf{W} \left(\mathbf{R} \,\vec{\theta}_{OC} + \Delta \,\vec{\kappa} \right) \right\|_{2} \to \min.$

 \rightarrow <u>Restrict</u> solution space to the "Range"

 $\operatorname{span}\left\{ \vec{u}_{i} \mid \sigma_{i} > \sigma_{cutoff} \right\}$

 \rightarrow n-dimensional solving strategies...

 \rightarrow KKT criterion to identify unique solution

intermingled nullspace

<u>orthogonal</u> nullspace

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 $\vec{\theta}^{(0)}$

 \mathcal{U}_{1}

WR





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 \rightarrow Solve

Constraints for Local Orbit Bumps

- Locality = minimise orbit impact ouside bump (ROI)
 - Choose correctors k surrounding bump monitors $\rightarrow \mathcal{H} = \{k\}$

$$\left\|\mathbf{U}_{B}^{T}\mathbf{W}_{B}\left(\mathbf{R}_{B}\vec{\theta}_{B}+\vec{\kappa}_{B,ref}\right)\right\|_{2}\rightarrow\min.$$

... under <u>restriction</u> of the solution space to

$$\operatorname{span}\left\{\vec{u}_{B,i} \mid \sigma_{B,i} > \sigma_{cutoff}\right\} \cap \operatorname{span}\left\{\mathbf{U}_{B}^{\mathrm{T}}\mathbf{W}_{B}\mathbf{R}_{B}\vec{V}_{B,i}^{*} \mid \vec{V}_{B,i}^{*} \in \mathbf{V}_{B}^{*}, i > 2\right\}$$

- $|\mathcal{H}|$ -2 column vectors $V_{B,l>2}^{*}$ of V_{B}^{*} corresponding to remaining SVs constitute ON-Basis for local orbit bumps (minimum impact outside ROI)

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- Dynamically choose as many correctors as needed
- Produce asked orbit offset ,without concern' of corr. lims.
- Provided as agent service to external clients



Exploitation of Nullspace (i)

• Use little orbit impact of ON-Base

span
$$\left\{ \vec{V_i} | \vec{V_i} \in \mathbf{V}, \sigma_i \leq \sigma_{cutoff} \right\}$$

to ease large corrector strengths in current setting $\vec{\theta}_0$:

ightarrow find $ec{ heta}_{\scriptscriptstyle C}$ such as to minimise

$$\left\| \mathbf{W}_{C} \left(\vec{\theta}_{C} + \vec{\theta}_{0} \right) \right\|_{2} \to \min.$$

with diagonal corrector weight matrix

$$\mathbf{W}_{C} \coloneqq \begin{pmatrix} w_{1}^{C} & 0 \\ & \ddots & \\ 0 & & w_{n}^{C} \end{pmatrix} \quad \leftarrow \text{ choose large weights } w_{j}^{C} \\ \text{ to put an emphasis on } \\ \text{ correctors } j \text{ to be eased} \end{cases}$$



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Exploitation of Nullspace (ii)

- ... again, use SVD to create a weighted DN-Base \boldsymbol{U}_{C} of correctors:



Bottom Line





Thanks for your attention



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